

- 1) Consider a Haynes-Shockley experiment on a p-type silicon bar. If a pulse of electrons is injected at  $x=0, t=0$ , and the maximum of the electron pulse reaches a probe at  $x=100\mu\text{m}$  at  $t=10\text{ ns}$ , determine electron mobility and diffusion coefficient using whatever method you like. Assume that a voltage of 10 V is maintained between the two ends of the 1 cm long bar.

$$\mathcal{E} = \frac{10\text{V}}{1\text{cm}} = 10^{1+2} \frac{\text{V}}{\text{m}} = 10^3 \frac{\text{V}}{\text{m}}$$

$$V_d = \frac{100\mu\text{m}}{10\text{ns}} = 10^{-4+8} \frac{\text{m}}{\text{s}} = 10^4 \frac{\text{m}}{\text{s}}$$

$$V_d = \mu \mathcal{E} \Rightarrow \mu = \frac{V_d}{\mathcal{E}} = \frac{10^4 \frac{\text{m}}{\text{s}}}{10^3 \frac{\text{V}}{\text{m}}} = \boxed{10^1 \frac{\text{m}^2}{\text{V}\cdot\text{s}} = \mu}$$

$$\frac{D}{\mu} = \frac{kT}{e} \Rightarrow D = \frac{kT}{e} \mu = 10^5 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$$

$$= \frac{1.38 \times 10^{-23} \cdot 300 \text{ J}}{1.6 \cdot 10^{-19} \text{ C}} \cdot 10^1 \frac{\text{m}^2}{\text{V}\cdot\text{s}} = \dots$$

Easier

$$= 0.029 \text{ V} \times 10^1 \frac{\text{m}^2}{\text{V}\cdot\text{s}} = \boxed{0.29 \frac{\text{m}^2}{\text{s}} = D}$$

$$= 2.9 \cdot 10^3 \frac{\text{cm}^2}{\text{s}}$$

2) Sketch the band diagram for an abrupt junction at thermal equilibrium for the following N-p junction: (N)  $\text{Al}_{0.35}\text{Ga}_{0.65}\text{As}$  doped so that  $E_C - E_F = 0.2 \text{ eV}$ ; (p) GaAs doped so that  $E_F - E_V = 0.1 \text{ eV}$ . Indicated clearly (qualitative):

- a. Which side has the larger depletion region
- b. Which side has the larger potential drop

Indicate quantitatively:

- c. Label quantitatively the difference between  $E_C$  on both sides
- d. Label quantitatively the difference between  $E_V$  on both sides

Other features only need to be drawn qualitatively.

$\text{GaAs } E_G = 1.42 \text{ eV}$

$\text{Al}_{0.35}\text{Ga}_{0.65}\text{As } E_G = 1.424 + 0.35 \times 1.247 \text{ eV}$

$1.247 \times 0.35 \approx 0.44$

$$\begin{array}{r} 1.25 \\ 0.3 \\ \hline .375 \end{array}$$

$$\begin{array}{r} 1.25 \\ .05 \\ \hline .0625 \end{array}$$

$$\begin{array}{r} .375 \\ .063 \\ \hline .438 \end{array}$$

$E_G = \begin{array}{r} 1.424 \\ .44 \\ \hline 1.864 \end{array} \approx 1.86 \text{ eV}$

$\Delta E_G = 0.44 \text{ eV}$

$\Delta E_V = 0.55 \times 0.35 \approx 0.165 + 0.028$

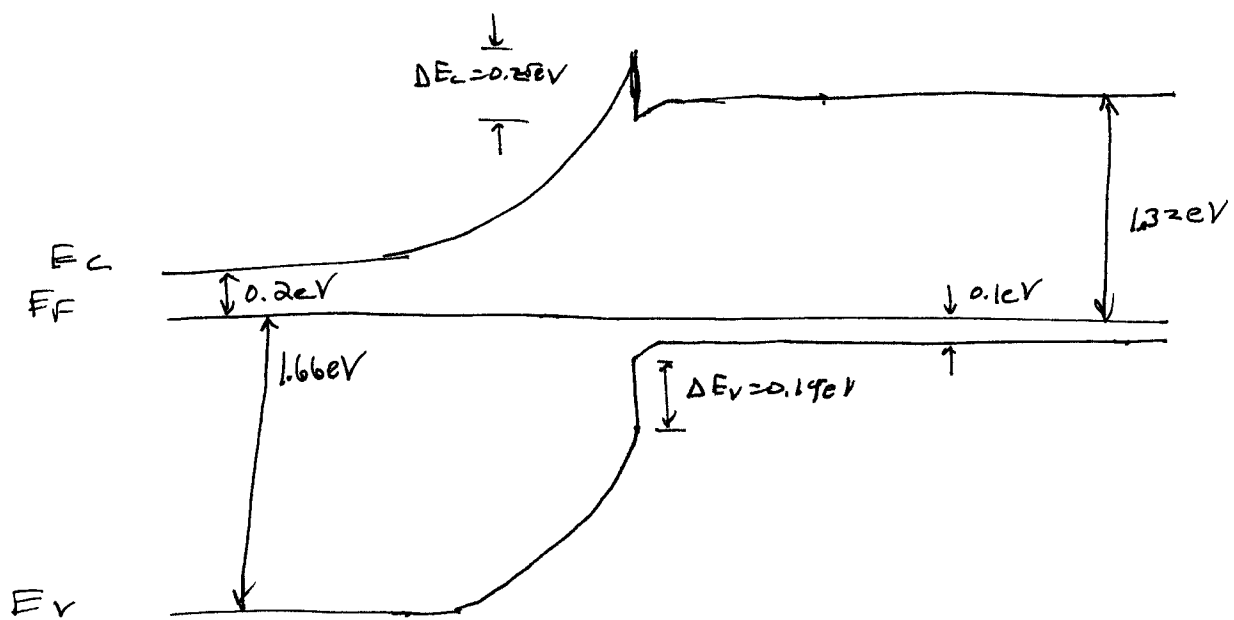
$$\begin{array}{r} 0.55 \\ 0.3 \\ \hline .165 \end{array}$$

$$\begin{array}{r} 0.55 \\ 0.05 \\ \hline 0.0275 \end{array}$$

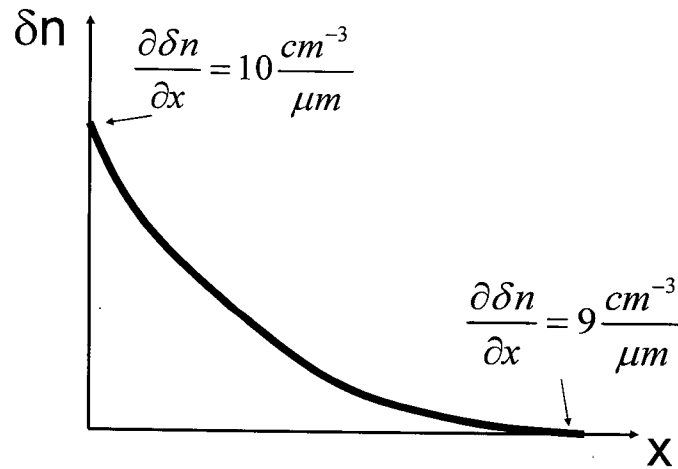
$\approx 0.19 \text{ eV}$

$\Delta E_C + \Delta E_V = \Delta E_G \Rightarrow \Delta E_C = 0.25 \text{ eV}$

Depletion region larger in lightly doped region = AlGaAs region.



- 3) For the hypothetical density of electrons in the p region of an npn transistor biased in active mode, find the value of  $\beta$ .



$$I_E \propto \left. \frac{d\delta n}{dx} \right|_{x=0}$$

$$I_C \propto \left. \frac{d\delta n}{dx} \right|_{x=W_B}$$

$$\Rightarrow \frac{I_E}{I_C} = \frac{10}{9} \Rightarrow I_E = \frac{1}{0.9} I_C$$

$$I_E = I_B + I_C$$

$$\Rightarrow I_C \frac{1}{0.9} = I_B + I_C$$

$$\Rightarrow \frac{I_C}{I_B} = \frac{1}{\frac{1}{0.9} - 1} = \boxed{9 = \beta}$$

4) What is the definition of the cutoff frequency?

Frequency at which  $\frac{i_{out}}{i_{in}} \equiv |h_{21}|$   
drops to unity (or 0dB).